

# Package: marble (via r-universe)

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**Type** Package

**Title** Robust Marginal Bayesian Variable Selection for Gene-Environment Interactions

**Version** 0.0.3

**Date** 2024-04-02

**Description** Recently, multiple marginal variable selection methods have been developed and shown to be effective in Gene-Environment interactions studies. We propose a novel marginal Bayesian variable selection method for Gene-Environment interactions studies. In particular, our marginal Bayesian method is robust to data contamination and outliers in the outcome variables. With the incorporation of spike-and-slab priors, we have implemented the Gibbs sampler based on Markov Chain Monte Carlo. The core algorithms of the package have been developed in 'C++'.

**Depends** R (>= 3.5.0)

**License** GPL-2

**Encoding** UTF-8

**URL** <https://github.com/xilustat/marble>

**LazyData** true

**LinkingTo** Rcpp, RcppArmadillo

**Imports** Rcpp, stats

**RoxygenNote** 7.3.1

**NeedsCompilation** yes

**Repository** <https://xilustat.r-universe.dev>

**RemoteUrl** <https://github.com/xilustat/marble>

**RemoteRef** HEAD

**RemoteSha** aab16def693da5400575c7482fdbf37acf9ebb91

## Contents

marble-package . . . . .	2
dat . . . . .	3
GxESelection . . . . .	4
marble . . . . .	5
print.GxESelection . . . . .	8
print.marble . . . . .	8

<b>Index</b>	<b>10</b>
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marble-package	<i>Robust Marginal Bayesian Variable Selection for Gene-Environment Interactions</i>
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## Description

In this package, we provide a set of robust marginal Bayesian variable selection methods for gene-environment interaction analysis. A Bayesian formulation of the quantile regression has been adopted to accommodate data contamination and heavy-tailed distributions in the response. The proposed method conducts a robust marginal variable selection by accounting for structural sparsity. In particular, the spike-and-slab priors are imposed to identify important main and interaction effects. In addition to the default method, users can also choose different structures (robust or non-robust), methods without spike-and-slab priors.

## Details

### PACKAGE

The user friendly, integrated interface **marble()** allows users to flexibly choose the fitting methods they prefer. There are two arguments in **marble()** that control the fitting method: **robust**: whether to use robust methods; **sparse**: whether to use the spike-and-slab priors to create sparsity. The function **marble()** returns a marble object that contains the posterior estimates of each coefficients. Moreover, it also provides a rank list of the genetic factors and gene-environment interactions. Functions **GxESelection()** and **print.marble()** are implemented for marble objects. **GxESelection()** takes a marble object and returns the variable selection results.

## References

- Lu, X., Fan, K., Ren, J., and Wu, C. (2021). Identifying Gene–Environment Interactions With Robust Marginal Bayesian Variable Selection. *Frontiers in Genetics*, 12:667074 [doi:10.3389/fgene.2021.667074](https://doi.org/10.3389/fgene.2021.667074)
- Ren, J., Zhou, F., Li, X., Ma, S., Jiang, Y. and Wu, C. (2020). Robust Bayesian variable selection for gene-environment interactions. [doi:10.1111/biom.13670](https://doi.org/10.1111/biom.13670)
- Zhou, F., Ren, J., Lu, X., Ma, S. and Wu, C. (2020). Gene–Environment Interaction: a Variable Selection Perspective. Epistasis. *Methods in Molecular Biology*. Humana Press (Accepted) <https://arxiv.org/abs/2003.02930>
- Wu, C., Cui, Y., and Ma, S. (2014). Integrative analysis of gene–environment interactions under a multi–response partially linear varying coefficient model. *Statistics in Medicine*, 33(28), 4988–4998 [doi:10.1002/sim.6287](https://doi.org/10.1002/sim.6287)

Shi, X., Liu, J., Huang, J., Zhou, Y., Xie, Y. and Ma, S. (2014). A penalized robust method for identifying gene–environment interactions. *Genetic epidemiology*, 38(3), 220-230 doi:10.1002/gepi.21795

Chai, H., Zhang, Q., Jiang, Y., Wang, G., Zhang, S., Ahmed, S. E. and Ma, S. (2017). Identifying gene-environment interactions for prognosis using a robust approach. *Econometrics and statistics*, 4, 105-120 doi:10.1016/j.ecosta.2016.10.004

## See Also

[marble](#)

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dat	<i>simulated data for demonstrating the features of marble.</i>
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## Description

Simulated gene expression data for demonstrating the features of marble.

## Usage

```
data("dat")
```

## Format

dat consists of four components: X, Y, E, clin.

## Details

### The data model for generating Y

Use subscript  $i$  to denote the  $i$ th subject. Let  $(Y_i, X_i, E_i, clin_i)$  ( $i = 1, \dots, n$ ) be independent and identically distributed random vectors.  $Y_i$  is a continuous response variable representing the phenotype.  $X_i$  is the  $p$ -dimensional vector of genetic factors. The environmental factors and clinical factors are denoted as the  $q$ -dimensional vector  $E_i$  and the  $m$ -dimensional vector  $clin_i$ , respectively. The  $\epsilon$  follows some heavy-tailed distribution. For  $X_{ij}$  ( $j = 1, \dots, p$ ), the measurement of the  $j$ th genetic factor on the  $i$ th subject, considering the following model:

$$Y_i = \alpha_0 + \sum_{k=1}^q \alpha_k E_{ik} + \sum_{t=1}^m \gamma_t clin_{it} + \beta_j X_{ij} + \sum_{k=1}^q \eta_{jk} X_{ij} E_{ik} + \epsilon_i,$$

where  $\alpha_0$  is the intercept,  $\alpha_k$ 's and  $\gamma_t$ 's are the regression coefficients corresponding to effects of environmental and clinical factors, respectively. The  $\beta_j$ 's and  $\eta_{jk}$ 's are the regression coefficients of the genetic variants and G×E interactions effects, correspondingly. The G×E interactions effects are defined with  $W_j = (X_j E_1, \dots, X_j E_q)$ . With a slight abuse of notation, denote  $\tilde{W} = W_j$ . Denote  $\alpha = (\alpha_1, \dots, \alpha_q)^T$ ,  $\gamma = (\gamma_1, \dots, \gamma_m)^T$ ,  $\beta = (\beta_1, \dots, \beta_p)^T$ ,  $\eta = (\eta_1^T, \dots, \eta_p^T)^T$ ,  $\tilde{W} = (\tilde{W}_1, \dots, \tilde{W}_p)$ . Then model can be written as

$$Y_i = E_i \alpha + clin_i \gamma + X_{ij} \beta_j + \tilde{W}_i \eta_j + \epsilon_i.$$

**See Also**[marble](#)**Examples**

```
data(dat)
dim(X)
```

---

GxESelection

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*Variable selection for a marble object*


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**Description**

Variable selection for a marble object

**Usage**

```
GxESelection(obj, sparse)
```

**Arguments**

obj	marble object.
sparse	logical flag. If TRUE, spike-and-slab priors will be used to shrink coefficients of irrelevant covariates to zero exactly.

**Details**

For class ‘Sparse’, the inclusion probability is used to indicate the importance of predictors. Here we use a binary indicator  $\phi$  to denote that the membership of the non-spike distribution. Take the main effect of the  $j$ th genetic factor,  $X_j$ , as an example. Suppose we have collected  $H$  posterior samples from MCMC after burn-ins. The  $j$ th G factor is included in the marginal  $G \times E$  model at the  $j$ th MCMC iteration if the corresponding indicator is 1, i.e.,  $\phi_j^{(h)} = 1$ . Subsequently, the posterior probability of retaining the  $j$ th genetic main effect in the final marginal model is defined as the average of all the indicators for the  $j$ th G factor among the  $H$  posterior samples. That is,  $p_j = \hat{\pi}(\phi_j = 1|y) = \frac{1}{H} \sum_{h=1}^H \phi_j^{(h)}$ ,  $j = 1, \dots, p$ . A larger posterior inclusion probability of  $j$ th indicates a stronger empirical evidence that the  $j$ th genetic main effect has a non-zero coefficient, i.e., a stronger association with the phenotypic trait. Here, we use 0.5 as a cutting-off point. If  $p_j > 0.5$ , then the  $j$ th genetic main effect is included in the final model. Otherwise, the  $j$ th genetic main effect is excluded in the final model. For class ‘NonSparse’, variable selection is based on 95% credible interval. Please check the references for more details about the variable selection.

**Value**

an object of class ‘GxESelection’ is returned, which is a list with components:

method	method used for identifying important effects.
effects	a list of indicators of selected effects.

## References

Lu, X., Fan, K., Ren, J., and Wu, C. (2021). Identifying Gene–Environment Interactions With Robust Marginal Bayesian Variable Selection. *Frontiers in Genetics*, 12:667074 doi:10.3389/fgene.2021.667074

## See Also

[marble](#)

## Examples

```
data(dat)
max.steps=5000
## sparse
fit=marble(X, Y, E, clin, max.steps=max.steps)
selected=GxESelection(fit,sparse=TRUE)
selected

## non-sparse
fit=marble(X, Y, E, clin, max.steps=max.steps, sparse=FALSE)
selected=GxESelection(fit,sparse=FALSE)
selected
```

---

marble

*fit a robust Bayesian variable selection model for G×E interactions.*

---

## Description

fit a robust Bayesian variable selection model for G×E interactions.

## Usage

```
marble(
  X,
  Y,
  E,
  clin,
  max.steps = 10000,
  robust = TRUE,
  sparse = TRUE,
  debugging = FALSE
)
```

## Arguments

X	the matrix of predictors (genetic factors). Each row should be an observation vector.
Y	the continuous response variable.
E	a matrix of environmental factors. E will be centered. The interaction terms between X (genetic factors) and E will be automatically created and included in the model.
clin	a matrix of clinical variables. Clinical variables are not subject to penalty. Clinical variables will be centered and a column of 1 will be added to the Clinical matrix as the intercept.
max.steps	the number of MCMC iterations.
robust	logical flag. If TRUE, robust methods will be used.
sparse	logical flag. If TRUE, spike-and-slab priors will be used to shrink coefficients of irrelevant covariates to zero exactly.
debugging	logical flag. If TRUE, progress will be output to the console and extra information will be returned.

## Details

Consider the data model described in "dat":

$$Y_i = \alpha_0 + \sum_{k=1}^q \alpha_k E_{ik} + \sum_{t=1}^m \gamma_t clin_{it} + \beta_j X_{ij} + \sum_{k=1}^q \eta_{jk} X_{ij} E_{ik} + \epsilon_i,$$

Where  $\alpha_0$  is the intercept,  $\alpha_k$ 's and  $\gamma_t$ 's are the regression coefficients corresponding to effects of environmental and clinical factors. And  $\beta_j$ 's and  $\eta_{jk}$ 's are the regression coefficients of the genetic variants and G×E interactions effects, correspondingly.

When sparse=TRUE (default), spike-and-slab priors are imposed to identify important main and interaction effects. If sparse=FALSE, Laplacian shrinkage will be used.

When robust=TRUE (default), the distribution of  $\epsilon_i$  is defined as a Laplace distribution with density  $f(\epsilon_i|\nu) = \frac{\nu}{2} \exp\{-\nu|\epsilon_i|\}$ , ( $i = 1, \dots, n$ ), which leads to a Bayesian formulation of LAD regression. If robust=FALSE,  $\epsilon_i$  follows a normal distribution.

Here, a rank list of the main and interaction effects is provided. For method incorporating spike-and-slab priors, the inclusion probability is used to indicate the importance of predictors. We use a binary indicator  $\phi$  to denote that the membership of the non-spike distribution. Take the main effect of the  $j$ th genetic factor,  $X_j$ , as an example. Suppose we have collected H posterior samples from MCMC after burn-ins. The  $j$ th G factor is included in the marginal G×E model at the  $j$ th MCMC iteration if the corresponding indicator is 1, i.e.,  $\phi_j^{(h)} = 1$ . Subsequently, the posterior probability of retaining the  $j$ th genetic main effect in the final marginal model is defined as the average of all the indicators for the  $j$ th G factor among the H posterior samples. That is,  $p_j = \hat{\pi}(\phi_j = 1|y) = \frac{1}{H} \sum_{h=1}^H \phi_j^{(h)}$ ,  $j = 1, \dots, p$ . A larger posterior inclusion probability  $j$ th indicates a stronger empirical evidence that the  $j$ th genetic main effect has a non-zero coefficient, i.e., a stronger association with the phenotypic trait. For method without spike-and-slab priors, variable selection is based on different level of credible intervals.

Both  $X$ ,  $clin$  and  $E$  will be standardized before the generation of interaction terms to avoid the multicollinearity between main effects and interaction terms.

Please check the references for more details about the prior distributions.

### Value

an object of class 'marble' is returned, which is a list with component:

posterior	the posterior samples of coefficients from the MCMC.
coefficient	the estimated value of coefficients.
ranklist	the rank list of main and interaction effects.
burn.in	the total number of burn-ins.
iterations	the total number of iterations.
design	the design matrix of all effects.

### References

Lu, X., Fan, K., Ren, J., and Wu, C. (2021). Identifying Gene–Environment Interactions With Robust Marginal Bayesian Variable Selection. *Frontiers in Genetics*, 12:667074 doi:10.3389/fgene.2021.667074

### See Also

[GxESelection](#)

### Examples

```
data(dat)

## default method
max.steps=5000
fit=marble(X, Y, E, clin, max.steps=max.steps)

## coefficients of parameters
fit$coefficient

## Estimated values of main G effects
fit$coefficient$G

## Estimated values of interactions effects
fit$coefficient$GE

## Rank list of main G effects and interactions
fit$ranklist

## alternative: robust selection
fit=marble(X, Y, E, clin, max.steps=max.steps, robust=TRUE, sparse=FALSE)
fit$coefficient
fit$ranklist
```

```
## alternative: non-robust sparse selection
fit=marble(X, Y, E, clin, max.steps=max.steps, robust=FALSE, sparse=FALSE)
fit$coefficient
fit$ranklist
```

---

print.GxESelection     *print a GxESelection object*

---

### Description

Print a summary of a GxESelection object

### Usage

```
## S3 method for class 'GxESelection'
print(x, digits = max(3, getOption("digits") - 3), ...)
```

### Arguments

x	GxESelection object.
digits	significant digits in printout.
...	other print arguments.

### Value

No return value, called for side effects.

### See Also

[GxESelection](#)

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print.marble     *print a marble object*

---

### Description

Print a summary of a marble object

### Usage

```
## S3 method for class 'marble'
print(x, digits = max(3, getOption("digits") - 3), ...)
```



**Arguments**

x	marble object.
digits	significant digits in printout.
...	other print arguments.

**Value**

No return value, called for side effects.

**See Also**

[marble](#)

# Index

- \* **datasets**
  - dat, [3](#)
- \* **models**
  - marble, [5](#)
- \* **overview**
  - marble-package, [2](#)
- clin (dat), [3](#)
- dat, [3](#), [6](#)
- E (dat), [3](#)
- GxESelection, [4](#), [7](#), [8](#)
- marble, [3-5](#), [5](#), [9](#)
- marble-package, [2](#)
- print.GxESelection, [8](#)
- print.marble, [8](#)
- X (dat), [3](#)
- Y (dat), [3](#)